

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
TOTAL	



General Certificate of Education  
Advanced Subsidiary Examination  
June 2013

# Mathematics

# MFP1

## Unit Further Pure 1

Friday 17 May 2013 9.00 am to 10.30 am

**For this paper you must have:**

- the blue AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

**Time allowed**

- 1 hour 30 minutes

**Instructions**

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

**Information**

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

**Advice**

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



J U N 1 3 M F P 1 0 1

Answer **all** questions.

Answer each question in the space provided for that question.

**1** The equation

$$x^3 - x^2 + 4x - 900 = 0$$

has exactly one real root,  $\alpha$ .

Taking  $x_1 = 10$  as a first approximation to  $\alpha$ , use the Newton–Raphson method to find a second approximation,  $x_2$ , to  $\alpha$ . Give your answer to four significant figures.

*(3 marks)*

QUESTION  
PART  
REFERENCE

**Answer space for question 1**







QUESTION  
PART  
REFERENCE

**Answer space for question 2**

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QUESTION  
PART  
REFERENCE

**Answer space for question 4**

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QUESTION  
PART  
REFERENCE

**Answer space for question 5**

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QUESTION  
PART  
REFERENCE

**Answer space for question 6**

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- 7 (a)** Show that the equation  $4x^3 - x - 540\,000 = 0$  has a root,  $\alpha$ , in the interval  $51 < \alpha < 52$ . (2 marks)
- (b)** It is given that  $S_n = \sum_{r=1}^n (2r - 1)^2$ .
- (i)** Use the formulae for  $\sum_{r=1}^n r^2$  and  $\sum_{r=1}^n r$  to show that  $S_n = \frac{n}{3}(kn^2 - 1)$ , where  $k$  is an integer to be found. (5 marks)
- (ii)** Hence show that  $6S_n$  can be written as the product of three consecutive integers. (2 marks)
- (c)** Find the smallest value of  $N$  for which the sum of the squares of the first  $N$  odd numbers is greater than 180 000. (2 marks)

QUESTION  
PART  
REFERENCE**Answer space for question 7**

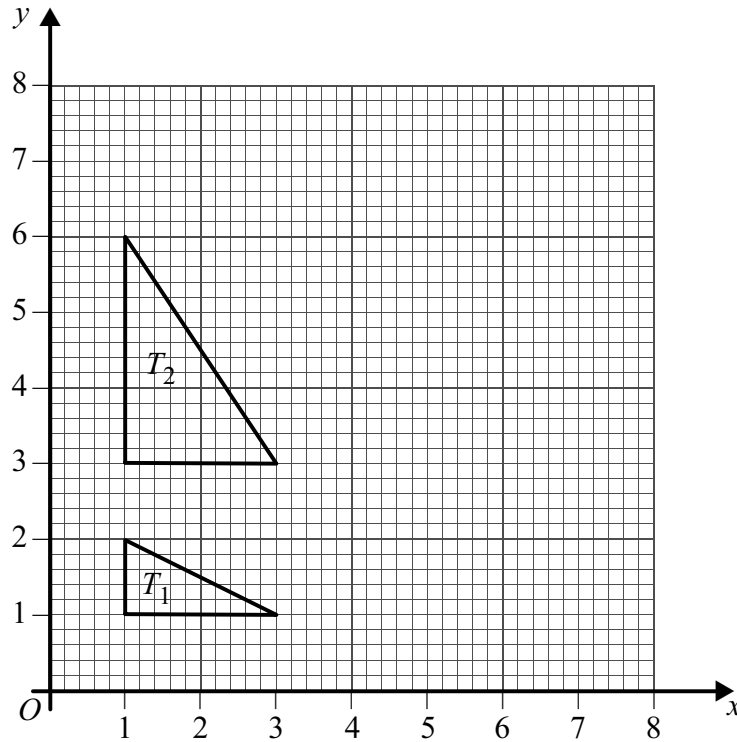
QUESTION  
PART  
REFERENCE

**Answer space for question 7**

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8 The diagram shows two triangles,  $T_1$  and  $T_2$ .



- (a) Find the matrix which represents the stretch that maps triangle  $T_1$  onto triangle  $T_2$ . (2 marks)
- (b) The triangle  $T_2$  is reflected in the line  $y = \sqrt{3}x$  to give a third triangle,  $T_3$ . Find, using surd forms where appropriate:
  - (i) the matrix which represents the reflection that maps triangle  $T_2$  onto triangle  $T_3$ ; (2 marks)
  - (ii) the matrix which represents the combined transformation that maps triangle  $T_1$  onto triangle  $T_3$ . (2 marks)

QUESTION  
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REFERENCE

Answer space for question 8

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QUESTION  
PART  
REFERENCE

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QUESTION  
PART  
REFERENCE

**Answer space for question 9**

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